**Figure 1**

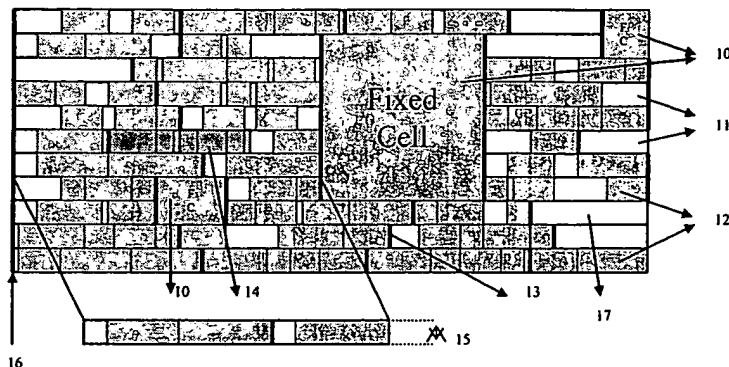


Figure 2

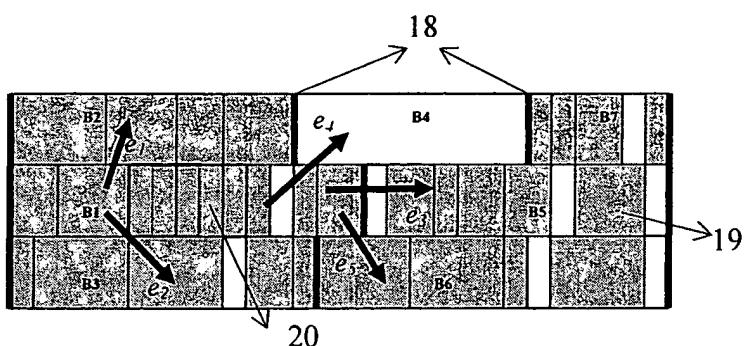
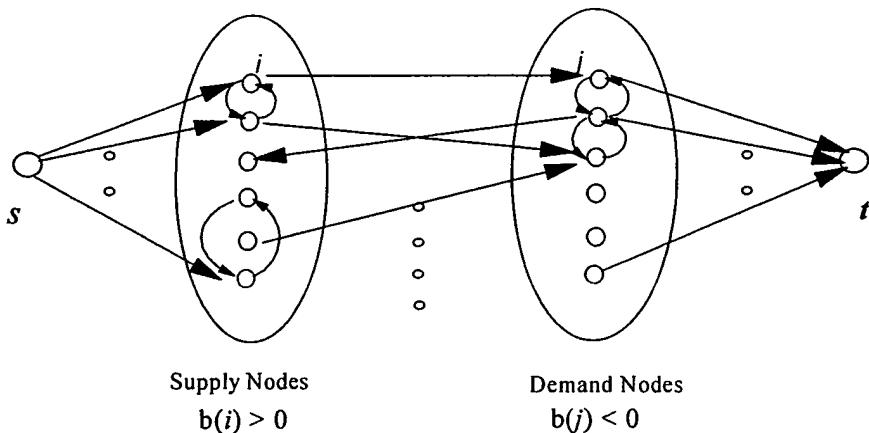


Figure 3



$\forall i$ if $b(i) > 0$,

$\text{Cap}(e_{si}) = b(i)$

$\text{Cost}(e_{si}) = 0$

$\forall i \neq s, j \neq t,$

$\text{Cap}(e_{ij}) = \text{Infinity}$ (Large Int)

$\text{Cost}(e_{ij}) = K e_{ij}$

$\forall j$ if $b(j) < 0$,

$\text{Cap}(e_{jt}) = -b(j)$

$\text{Cost}(e_{jt}) = 0$

\forall : Notation represents the meaning "For Every Element"

\in : Notation represents the meaning "Element of"

Figure 4

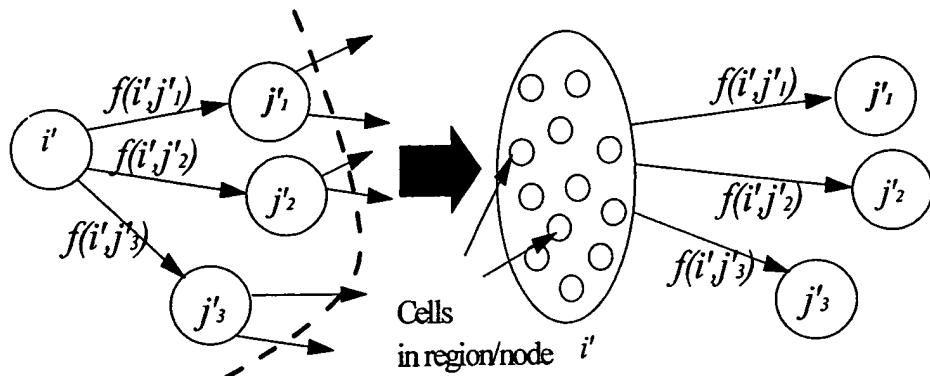
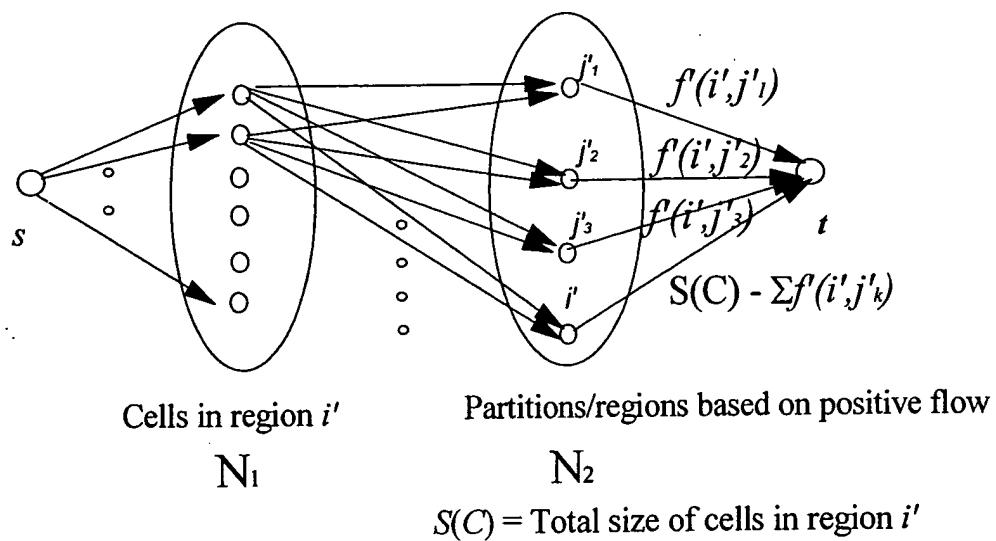


Figure 5



$\forall i \in N_1$
 $\text{Cap}(e_{si}) = 1$
 $\text{Cost}(e_{si}) = 0$

$\forall i \in N_1, j \in N_2$,
 $\text{Cap}(e_{ij}) = 1$
 $\text{Cost}(e_{ij}) = \text{Cost of moving}$
 $\text{cell } i \text{ to region } j$
 $\text{multiplier } \mu_{ij} = \text{size of cell } i$

$\forall j \in N_2$
 $\text{Cap}(e_{jt}) = \text{flow to region } j$
 $\text{Cost}(e_{jt}) = 0$

\forall : Notation represents the meaning "For Every Element"
 \in : Notation represents the meaning "Element of"

Figure 6

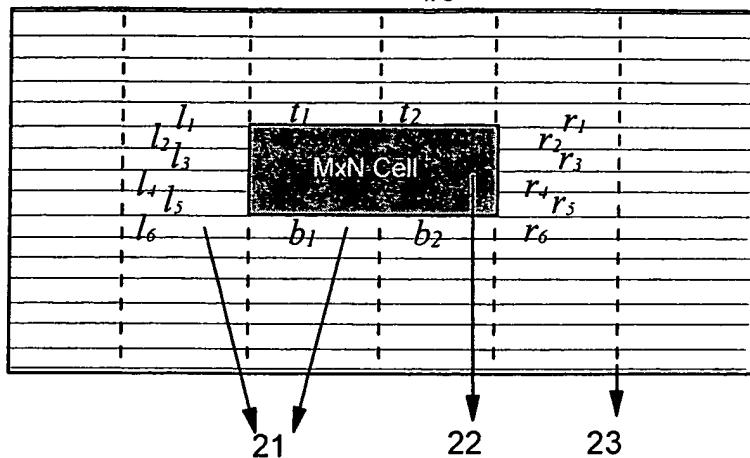
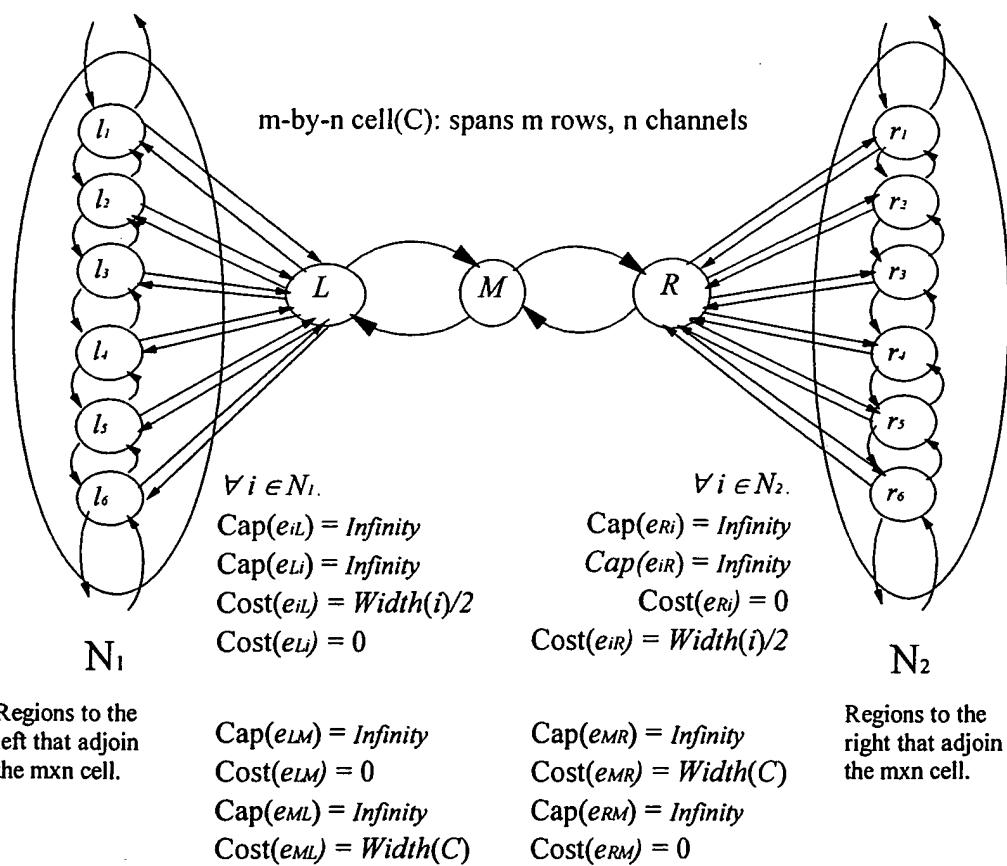


Figure 7



\forall : Notation represents the meaning "For Every Element"

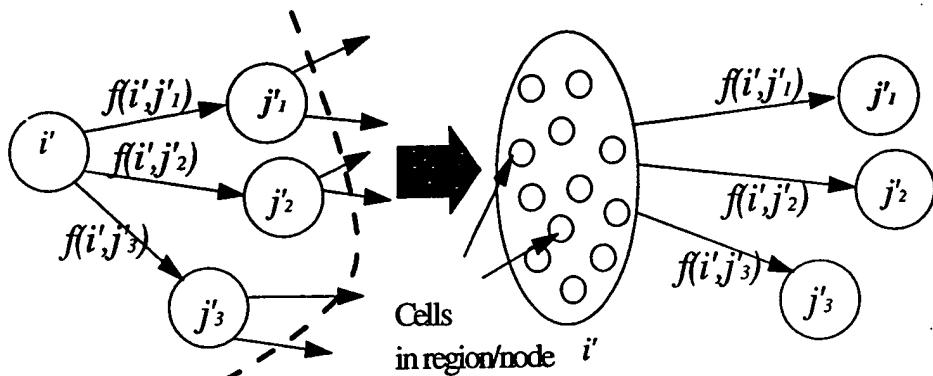
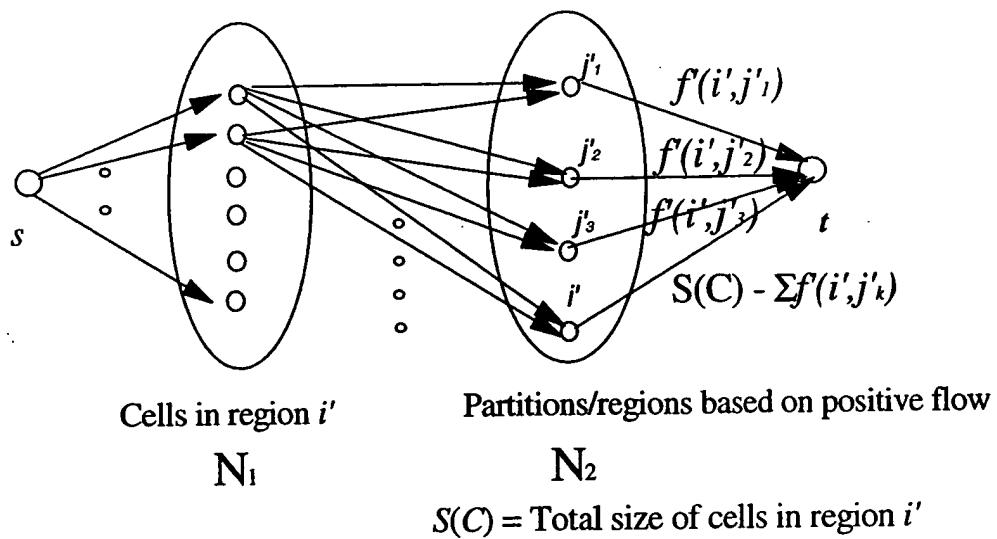


Figure 5



$\forall i \in N_1$	$\forall i \in N_1, j \in N_2,$	$\forall j \in N_2$
$\text{Cap}(e_{si}) = 1$	$\text{Cap}(e_{ij}) = 1$	$\text{Cap}(e_{ji}) = \text{flow to region } j$
$\text{Cost}(e_{si}) = 0$	$\text{Cost}(e_{ij}) = \text{Cost of moving}$ $\text{cell } i \text{ to region } j$	$\text{Cost}(e_{ji}) = 0$
	$\text{multiplier } \mu_i = \text{size of cell } i$	

\forall : Notation represents the meaning "For Every Element"
 \in : Notation represents the meaning "Element of"

Figure 6

```

Placement_Aware_Region_Definition ()
Begin
 1 Build placement image
 2 For each circuit row  $r$  in the layout
    Begin
      3   scanline_x = row_xlow ( $r$ ); last_region_boundary = row_xlow ( $r$ );
      4   leading_free_space = false;
      5    $S$  = sorted list of cells in row  $r$  by increasing position along  $x$ -direction
      6    $c$  = first cell in sorted list  $S$ 
      7   while ( $c$ )
        Begin
          8     If ( $xpos(c) > scanline_x$ )
            Begin
              9       If ( $xpos(c) - last\_region\_boundary > W$ )
                Begin
                  10       $p$  = create_region ( $r, last\_region\_boundary + W, last\_region\_boundary$ )
                  11      scanline_x = ( $last\_region\_boundary + W$ )
                End
              12      Else
                Begin
                  13        If (is_fixed_cell( $c$ ) || is_blockage( $c$ ) || leading_free_space)
                    Begin
                      14           $p$  = create_region ( $r, xpos(c), last\_region\_boundary$ )
                      15          scanline_x = last_region_boundary = xpos( $c$ )
                      16          leading_free_space = false
                    End
                  17        Else if ( $xpos(c) - scanline_x \geq 0.50 * W$  and  $scanline_x > last\_region\_boundary$ )
                    Begin
                      18           $p$  = create_region ( $r, scanline_x, last\_region\_boundary$ )
                      19          last_region_boundary = scanline_x
                      19          leading_free_space = true
                    End
                  20        Else
                    scanline_x =  $xpos(c)$ 
                  End
                End
              21      Else if ( $xpos(c) == scanline_x$ )
                Begin
                  22        If (is_fixed_cell( $c$ ) || is_blockage( $c$ ))
                    Begin
                      23           $p$  = create_region ( $r, xpos(c) + width(c), scanline_x$ )
                      24          scanline_x += width( $c$ )
                      25          last_region_boundary = scanline_x
                    End
                  26        Else if (is_movable_cell( $c$ ))
                    Begin
                      27          If ( $xpos(c) + width(c) \leq W$ )
                        scanline_x += width( $c$ )
                      28          Else
                        Begin
                          29                           $p$  = create_region ( $r, xpos(c) + width(c), last\_region\_boundary$ )
                          30                          last_region_boundary = scanline_x
                          31                          scanline_x += width( $c$ )
                        End
                      32                    End
                    End
                  33                   $c$  = next cell in the sorted list  $S$ 
                End
              End
            End
          End
        End
      End
    End
  End
End

```

FIGURE 9

Global_Area_Migration_Graph ($G(V,E)$)**Begin**

1. $V = \{\text{regions}\}$, $E = \{\text{edge between neighboring regions}\}$
2. $\forall e \in E, \text{Cost}(e) = K_e$
3. $\forall e \in E, \text{Cap}(e) = \text{Infinity}$ (Large integer)
4. $\forall v \in V, \text{Size}(v) = \text{Total size of movable cells in } v$
5. $\forall v \in V, \text{Cap}(v) = \text{Total available space for movable cells in } v \text{ (i.e. region)}$
6. $\forall v \in V, b(v) = \text{Size}(v) - \text{Cap}(v)$
7. If $b(v) > 0$, v is a supply node.
8. If $b(v) < 0$, v is a demand node.
9. If $b(v) = 0$, v is a transshipment node.

End \forall : Notation represents the meaning "*For Every Element*" \in : Notation represents the meaning "*Element of*"**Figure 10**

Generalized_Flow_Graph (region i')**Begin**

1. $N_1 = \{\text{cells in region } i'\}, N_2 = \{i'\} \cup \{\text{neighboring regions}\}$
2. $E = \{\text{edge representing cell-to-region assignment}\}$
3. $S(N_1) = \text{Total size of cells in } N_1 \text{ (region } i')$
4. $\text{Smallest}(N_1) = \text{Smallest cell size in } N_1 \text{ (region } i')$
5. *Introduce an edge from N_1 to N_2 for every possible cell-to-region assignment,*

$$\forall i \in N_1, j \in N_2, \text{Cap}(e_{ij}) = 1$$

$$\forall i \in N_1, j \in N_2, \text{multiplier, } \mu_{ij} = \text{size of cell } i$$

$$\forall i \in N_1, j \in N_2, \text{Cost}(e_{ij}) = \text{Cost of moving cell } i \text{ to region } j$$

6. *Introduce source node s , with edges such that*

$$\forall i \in N_1, \text{Cap}(e_{si}) = 1$$

$$\forall i \in N_1, \text{Cost}(e_{si}) = 0$$

7. *Introduce sink node t , with edges such that*

$$\forall j \in N_2, \text{Cap}(e_{jt}) = f'(i', j) = \text{MAX}(\text{Smallest}(N_1), f(i', j)), \text{If } f(i', j) > 0 \\ 0, \text{Otherwise}$$

$$\forall j \in N_2, \text{Cost}(e_{jt}) = 0$$

End

\forall : Notation represents the meaning "For every element"

\in : Notation represents the meaning "Element of" (a set theory notation)

Figure 11